# Unsupervised color coding for visualizing image classification results 

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#### Abstract

In this article, we describe a general purpose system that, given as input a segmented/classified image, automatically provides different visual outputs exploiting solid colors, color boundaries, and transparent colors. Moreover, if the names of the classes are given, the system automatically places a textual label in the less salient sub-region of the corresponding class. For color-class association and class label placement, we take into account the underlying image color and structure exploiting both saliency and superpixel representation. The color selection and the color-class association are formulated both as optimization problems and heuristically solved using a Local Search procedure. Results show the effectiveness of the proposed system on images having different content and different number of annotated regions.


## Keywords

Image segmentation, high-contrast colors, color-class association, optimization

## Introduction

In image segmentation and classification applications, the user may want to visually code and associate ancillary information, such as names, to the different classes depicted in the image. The decision of how to visually code the different classes and eventually where to place the textual annotations is a problem often referred as view management. ${ }^{1}$ Such a problem commonly arises in different domains, such as visual retrieval, ${ }^{2}$ video surveillance, ${ }^{3}$ medical imaging, ${ }^{4,5}$ cartography, ${ }^{6}$ remote sensing, ${ }^{7}$ and augmented reality. ${ }^{8}$ Among visual features, color is widely employed to visualize the output of a segmentation-classification process. While in some applications, the color-class association is strongly driven by conventions (e.g. in cartography), in many other domains this process cannot be easily automated since there are no consolidated conventions or common guidelines. While several heuristic procedures have been proposed to select high-contrast color palettes (see the following section), the problem of color-class association is not completely solved as a serious problem arises because the chosen colors must be displayed together and
assigned to classes that maybe spatially adjacent. In practice, this is mainly based on a trial-and-error approach and demands a concerted effort on the part of the user. In many dynamic applications (e.g. augmented reality, video surveillance) or when very large datasets have to be processed, ${ }^{9-11}$ this activity should be automated as much as possible.

In this work, we propose a general purpose system that, given as input a segmented/classified image, provides different visual outputs exploiting solid colors, color boundaries and transparent colors. In the first case, each class is filled with the associated color, thus resulting in a pseudo-color representation of the image; in the second case, colored region boundaries are displayed on the original image; in the third case,

[^0]transparent colors are overlaid on the original image. For the second and third outputs, class labels (if available) are automatically placed. In the overlay solutions, to select the colors and to place class names, we take into account the underlying color distribution and structure of the image using both a superpixel representation and saliency map. Both the label placement and the high-contrast color selection problems are NPhard. ${ }^{12,13}$ In this work, we model them as optimization problems and describe a method for heuristically solving them using a Local Search (LS) procedure.

The main contributions of this work are as follows:

- The introduction of a new general purpose system able to provide different visual outputs exploiting solid colors, color boundaries, and transparent colors. The system is completely unsupervised and its core is constituted by algorithms able to work in any color space, with any color distance, and with any color palette.
- Introduction of the use of transparent colors by taking into account underlying image colors, in order to maximize visibility in all the use cases in which the system can be used.
- The formalization of the high-contrast color selection and color-class association as a single problem, and the design of an efficient optimization algorithm to solve it.
- A systematic way to automatically find the best locations where to place class labels.
- The possibility to download the system (http:// www.ivl.disco.unimib.it/activities/cc4visual-im-class-results/) and easily expand its functionalities.


## Related work

The great majority of the automatic approaches in the state of the art consist of heuristic procedures proposed to define high-contrast sets of colors without considering their association to the image classes (leaving color-class association to the user). For example, Kelly ${ }^{14}$ conceived a list of 22 maximally contrasting surface colors, such that each color of the list is maximally different from the one immediately preceding it. Later Carter and Carter ${ }^{15}$ formulated the first algorithm to compute easily discriminable sets of colors. Several authors ${ }^{16-20}$ have devised algorithms that can also fulfill a number of ergonomical requirements. In 1995, Campadelli et al. ${ }^{21}$ presented an abstract formulation of the problem of selecting high-contrast color sets, defining it as a combinatorial optimization problem on graphs. More recently, Carter and Huertas ${ }^{22}$ have studied the ability of different metrics and several color spaces to enhance the discriminability of small
visual targets with ultra-large color differences. Glasbey et al. ${ }^{23}$ proposed a greedy method for the selection of set of colors for categorical image and showed that its performance is comparable with that of a simulated annealing algorithm. Breslow et al. ${ }^{24}$ proposed an algorithm for generating color scales for both categorical and ordinal coding; their method uses a positional space partition strategy to generate a lightness scale and then applies the method developed from Campadelli et al. ${ }^{13}$ to select discriminable colors according to the lightness constraint. Rodriguez-Pardo and Sharma ${ }^{25}$ proposed a dynamical solution to the problem using a hierarchical clustering followed by a simple truncation to select the desired number of high-contrast colors at run time. Radlak and Smolka ${ }^{26}$ proposed a methodology for deriving optimized visualization based on maximizing local distance between colors. They present visualization results using a new color contrast measure optimized with a genetic algorithm (GA). Their method can be used to obtain pseudo-color encoded images of segmentation results.

Concerning color-class association, as an alternative to automatic approaches, some interactive systems for color coding have been also proposed. ${ }^{27-31}$ They share the idea of using a fixed color palette of high-contrast colors and rely on the user intervention to associate them to the image classes. In this article instead, both the search of a high-contrast set of colors and the color-class association are performed automatically together with the placement of the class label.

## The proposed system

The processing pipeline of the proposed system is reported in Figure 1. Given an image to be coded, its classification/segmentation, the set of available colors (in the following, color palettes), and (optionally) the labels of the classes, the system generates different proposals ranging from solid color solutions (see Figure 1 (a) and (b)) to color boundary and transparent color overlay solutions (see Figure 1(c) and (d)). For the latter solutions, the optimal locations for the region labels are also produced in output.

Each proposal depends on the input palette, the number, and the spatial relationship of the classes in the image to be coded. To generate such proposals, the problem of selecting high-contrast color sets is jointly addressed with the color-class association problem, in order to maximize the color discriminability among adjacent classes. For color boundary and transparent color overlay solutions, a further problem is faced: the chosen colors have also to be at maximum contrast with respect to the underlying image colors. Finally, to place the class labels, the less salient sub-region able to


Figure 1. Workflow of the proposed system.
contain the entire label must be found for each class. To take into account the content of the image to be coded and the spatial relationship of the classes, suitable image descriptions in terms of superpixel representation, saliency, and class adjacency representation are exploited.

The proposed system takes as input an RGB image $I$, its segmented/classified version $R$ with class regions $r_{1}, \ldots, r_{n}$, the color palette $C$, and the class labels $l_{i}$, $i=1, \ldots, n$. The first stage consists in the computation of the superpixel map $S,{ }^{32,33}$ which is composed by superpixels $s_{1}, \ldots, s_{m}$, and the computation of the saliency map $M$. The superpixel representation is used since the number of pixels is high even at moderate resolutions, making the optimization on the level of
pixels intractable. ${ }^{33}$ Superpixels instead are local, coherent, and preserve most of the structure. In this work, we followed Mori et al. ${ }^{33}$ which applied Normalized Cuts algorithm ${ }^{34}$ to produce the superpixel map. An example of superpixel map is shown in Figure 2(d). Saliency intuitively characterizes some parts of the image that appear to an observer to stand out relative to their neighboring parts. ${ }^{35}$ In this work, we use saliency to detect which are, for each region, the locations of the least prominent parts. These are the candidate locations to place the class label. To compute the saliency map in this work we use the method proposed in Zhang and Sclaroff. ${ }^{36}$ It is a Boolean map-based saliency model which leverages global topological cues that are known to help in


Figure 2. (a) Original image, (b) image segments, (c) saliency map, (d) superpixel map, (e) superpixels belonging to $I_{1}$, that is, the inside of region $r_{1}$, and ( $f$ ) superpixels belonging to $O_{1}$, that is, the outside of the same region.
perceptual figure-ground segregation. The model is based on the surroundedness cue taken from Gestalt psychological studies. An example of saliency map is shown in Figure 2(c).

Both $S$ and $M$ are computed from $I$. The segmented image $R$ is used to compute the region adjacency graph (RAG). The adjacency matrix $A$ is obtained from the RAG: the element $A_{(i, k)}$ is set to 1 if nodes $i$ and $j$ are connected in the RAG (i.e. the regions $r_{i}$ and $r_{j}$ are adjacent in $R$ ) and set to $\infty$ otherwise.

The looping on the regions then begins. For each region $i=1, \ldots, n$, all the superpixels $s_{j} \cap r_{i}$ are found, and the sets $I_{i}, O_{i}$ are initialized to the empty set, that is, $I_{i}=O_{i}=\emptyset$. For each superpixel $s_{j}$, a $k$-means clustering on the RGB values of the pixels identified by positions $\mathbf{x} \in I \cap s_{j}$ is run with $k=2$ to find the two color centroids $c_{1}$ and $c_{2}$. If the distance between colors $c_{1}$ and $c_{2}$ is less than a fixed threshold $t$, then their average is added to the set of colors $I_{i}$, otherwise both $c_{1}$ and $c_{2}$ are added

$$
I_{i}= \begin{cases}I_{i}=I_{i} \cup \operatorname{mean}\left(c_{1}, c_{2}\right) &  \tag{1}\\ \text { if } d\left(c_{1}, c_{2}\right)<t \\ I_{i}=I_{i} \cup c_{1} \cup c_{2} & \\ \text { otherwise }\end{cases}
$$

The pixels of the saliency map $M$ corresponding to the current region $r_{i}$ are then filtered using a box filter $b_{i}$ having dimensions $\left[w_{i}, h_{i}\right]$, which are defined by the size of the label $l_{i}$ assigned to the corresponding class. In order to avoid as much as possible to the label to stick out from the current region, a modified version of $M$ is computed

$$
M^{\prime}(\mathbf{x})= \begin{cases}M^{\prime}(\mathbf{x}) & \text { if } \mathbf{x} \in r_{i}  \tag{2}\\ P & \text { otherwise }\end{cases}
$$

If $i>1, M^{\prime}$ is updated by setting to $P$ the label locations for the regions $r_{j}, j<i$ in order to avoid overlapping labels. The new map $M^{\prime}$ is used to produce the
output $B_{i}=b_{i} * M^{\prime}$. The location $L_{i}$ where to place the label for region $r_{i}$ is then found as

$$
\begin{equation*}
L_{i}=\arg \min _{\mathbf{x}} B_{i}(\mathbf{x}) \tag{3}
\end{equation*}
$$

By design, only one label for each class is placed. In case of classes composed of multiple regions, the label is placed only in the largest region in the less salient part.

The next step is the identification of the part of the image adjacent to $r_{i}$, that is, the set of pixels neighboring with $r_{i}$. To this end, the dilation mathematical morphology operator is applied to $r_{i}$ to obtain $d r_{i}$. The region $n r_{i}$, representing the adjacent space external to region $r_{i}$ is then obtained as $n r_{i}=d r_{i}-r_{i}$. The superpixels $s_{j} \in n r_{i}$ are then found, and for each superpixel, the two centroids $c_{1}$ and $c_{2}$ are found. As for $I_{i}, O_{i}$ is updated as follows

$$
O_{i}= \begin{cases}O_{i}=O_{i} \cup \operatorname{mean}\left(c_{1}, c_{2}\right) & \text { if } d\left(c_{1}, c_{2}\right)<t  \tag{4}\\ O_{i}=O_{i} \cup c_{1} \cup c_{2} & \text { otherwise }\end{cases}
$$

The final stage of the proposed system is to find a set of colors $c_{i}, i=1, \ldots, n$ (one for each image class), $\left\{c_{i}\right\}_{i=1}^{N} \in C$ having maximum contrast between them, and with the colors $I_{i}, O_{i}, i=1, \ldots, n$. This is done using the high-contrast coloring (HCC) algorithm described in the next subsection.

The pseudo-code of the algorithm implemented in the proposed system is given in algorithm 1.

## HCC algorithm

Given a palette $C$ of possible colors and the sets of colors, respectively, inside and outside each region $r_{i}$, that is, $I_{i}$ and $O_{i}, i=1, \ldots, n$, the problem is to find a set of $n$ colors having maximum contrast among them and

Algorithm 1 Pseudo-code of the algorithm implemented in the proposed system.

> Data: RGB image $I$, segmented image
> $R=\bigcup_{i=1}^{N} r_{i}$, color palette(s) $P$, region
> labels $\left\{l_{i}\right\}_{i=1}^{N}$
> Result: colors $C_{i}$, label locations $L_{i}$, $i=1, \ldots, N$
> Compute saliency map $M$
> Compute superpixel segmentation $S$
> Initialize adjacency matrix $A=\operatorname{Inf}(N, N)$
> for each region $r_{i} \in R, i=1$ to $N$ do
> $I_{i}=O_{i}=\emptyset$
> $M^{\prime}=M$
> Find superpixels $s_{k} \in r_{i}$
> for each superpixel $s$ do
> Set $M^{\prime}(x)=P$ for each $x \in s$
> Run clustering on RGB colors to find 2
> centroids $c_{1}$ and $c_{2}$
> if $d\left(c_{1}, c_{2}\right)<t$ then
> $I_{i}=I_{i} \cup \operatorname{mean}\left(c_{1}, c_{2}\right)$
> else
> $\left\llcorner I_{i}=I_{i} \cup c_{1} \cup c_{2}\right.$
> if $i>1$ then
> for $j=1, \ldots, i-1$ do
> Set $M^{\prime}(x)=P$ for each $x \in\left[L_{j}, L_{j}+w\right] \times\left[L_{j}, L_{j}+h\right]$
> $d r_{i}=\operatorname{dilate}\left(r_{i}\right)$
> Find superpixels $s_{k} \in n r_{i}=d r_{i}-r_{i}$
> for each superpixel $s$ do
> Run clustering on RGB colors to find 2
> centroids $c_{1}$ and $c_{2}$
> if $d\left(c_{1}, c_{2}\right)<t$ then
> $O_{i}=O_{i} \cup \operatorname{mean}\left(c_{1}, c_{2}\right)$
> else
> $L O_{i}=O_{i} \cup c_{1} \cup c_{2}$
> Find regions $r_{j}, j=\{1, \ldots, N\}-i$ s.t.
> $r \cap d r_{i} \neq \emptyset$
> if $\neg \operatorname{isempty}(j)$ then
> $\left\llcorner A_{(i, j)}=1\right.$
> $B=\operatorname{boxfilter}\left(M^{\prime}, h, w\right)$
> Find $L_{i}$ s.t. $L_{i}=\arg \min _{x \in r_{i}} B$
> Find $N$ high contrast colors wrt
> $A, I_{i}, O_{i}, i=1, \ldots, N$ that maximize Eq. 5
with respect to $I_{i}$ and $O_{i}$ and to place them so that the local contrast is maximized. Formally

$$
\begin{align*}
& c_{1}, \ldots, c_{n}=\arg \max _{c_{1}^{*}, \ldots, c_{n}^{*}} \min \left(\left[\min _{\substack{j=1, \ldots, n \\
k=1, \ldots, n \\
j \neq k}} d\left(c_{j}^{*}, c_{k}^{*}\right),\right.\right. \\
& \min _{\substack{j=1, \ldots, n \\
k=1, \ldots, n \\
j \neq k}} A_{(j, k)} d\left(c_{j}^{*}, c_{k}^{*}\right), \min _{\substack{i=1, \ldots, n \\
j=1, \ldots,\left|I_{i}\right|}} d\left(c_{i}^{*}, I_{i}\{j\}\right),  \tag{5}\\
& \left.\left.\min _{\substack{i=1, \ldots, n \\
j=1, \ldots,\left|O_{i}\right|}} d\left(c_{i}^{*}, O_{i}\{j\}\right)\right] \circ\left[w_{d}, w_{A}, w_{I}, w_{O}\right]^{-1}\right)
\end{align*}
$$

where the operator $\{\cdot\}$ is used to index elements inside a set, $|\cdot|$ is the set cardinality, and ${ }^{\circ}$ is used to denote
the Hadamard product. The first term in the righthand side of equation (5) computes the minimum distance among the selected colors, the second one the minimum distance between the colors corresponding to adjacent regions, the third one the minimum distance between the color associated with the region $r_{i}$ and the colors inside it (i.e. $I_{i}$ ), and the fourth one the minimum distance between the color associated with the region $r_{i}$ and the colors outside it (i.e. $O_{i}$ ).

Some of the possible outputs are reported in Figure 1. They are obtained by acting on the weights $\left[w_{d}, w_{A}, w_{I}, w_{O}\right]$, as reported in Table 1.

The optimization problem is solved with the LS procedure introduced in Bianco and Citrolo. ${ }^{37}$ The LS procedure is based on the concept of neighborhood, which is defined as follows

$$
\begin{equation*}
N_{h}(K)=\{\tilde{K} \subset C:|K \backslash \tilde{K}|=h, h<n,|\tilde{K}|=n\} \tag{6}
\end{equation*}
$$

In this work the 1 -neighborhood $N_{1}(\cdot)$ is used, which means that two solutions are 1-neighbors if and only if they differ for just one element. Starting from a random solution with $n$ colors, in each iteration, an exhaustive search over the 1-neighborhood of the current solution is performed: the solution that leads to the highest improvement according to equation (5) is selected as the new current solution. The optimization ends when no improved solution is found. In order to speed-up convergence, the solution is initialized using grid search. Starting from the image region $r_{1}, c_{1}$ is chosen to solve equation (5) by setting $\left[w_{d}, w_{A}\right.$, $\left.w_{I}, w_{O}\right]=\left[0,0, w_{I}, w_{O}\right]$ and $n=1$. For image regions from $r_{2}$ to $r_{n}$, new elements are added to the solution by solving equation (5) and keeping fixed the previous elements.

## Experimental results

The proposed method can work with any color palette having any cardinality, described in any color space given that a color distance is defined. The default color palette is the Munsell Atlas which contains over 1300 colors. This choice is due to the fact that the classified images may not only be displayed on the screen but also printed. Since the gamuts of feasible colors of common displays and color printers differ considerably, a high-contrast color coding on the screen may be drastically modified when printed. Since many colors cannot be reproduced in print, restricting the selection of color to the Munsell Atlas greatly limits this drawback. ${ }^{30}$

Three other different color palettes $C$ among which to select the $n$ colors are used in the following. They have been chosen as can be easily visualized and appreciated as a whole. The three color palettes are reported

Table 1. Output obtained with different parameter settings in equation (5).

| Parameters | Output obtained |
| :--- | :--- |
| $\left[w_{d}, w_{A}, w_{l}, w_{0}\right]$ | Solution taking into account the original image colors inside each region. Suggested when region <br> boundaries have to be displayed or colors have to be overlaid on the original image. |
| $\left[w_{d}, w_{A}, 0,0\right]$ | Solution ignoring the original image colors. Suggested when a pseudo-color representation of the <br> image is needed. |
| $\left[w_{d}, 0,0,0\right]$ | Solution ignoring the original image colors and region adjacency. Suggested when only a set of <br> maximally contrasting colors is needed (e.g. Bianco and Citrolo ${ }^{37}$ ). |



Figure 3. Color palettes used in this work: (a) gray-scale, (b) iso-luminance, and (c) web-safe.
in Figure 3. These palettes have different color characteristics: the first one varies only in luminance, and thus it is inherently one-dimensional (1D); the second one is two-dimensional (2D) as representing a sampling of an iso-luminance plane in the CIELab color space; ${ }^{38}$ and the third one is three-dimensional (3D) as spanning the whole RGB cube. The first palette is a gray-scale composed of 256 shades of gray, that is, $|C|=256$. The second one contains iso-luminance colors, with $|C|=441$. The third one corresponds to the palette of web-safe colors, with $|C|=216$. The web-safe palette was defined as a set of colors that could be shown without dithering on 256 -color displays. In fact, on 256-color displays, applications can set a palette of any selection of colors that they choose, dithering the rest.

We report in Figure 4 the colors selected for the three palettes for different set cardinalities $n=3,4,6,9,12$ without considering the spatial layout, that is, setting $\left[w_{d}, w_{A}, w_{I}, w_{O}\right]=[1,0,0,0]$ in equation (5). It is possible to see that when $n$ increases, the selected colors tend to be more similar. This explains the importance of the spatial layout of the colors on the image, that is, the way in which the colors are associated with the image regions, which is captured by the second term in equation (5).

Some example results taking into account the image spatial layout and color-class associations are reported for different application domains: Pascal VOC 2012
segmentation challenge, ${ }^{39}$ texture classification, images annotation, and webpage layout segmentation. For all examples, the distance $d(\cdot, \cdot)$ used is the CIE $\Delta E$ which is an Euclidean distance computed in the CIELab color space. The CIELab color space is chosen in this work for its popularity and simplicity, ${ }^{40}$ but other color spaces could be used in the proposed system as well, as for example the CIECAM02 ${ }^{41}$ and its extensions ${ }^{42}$ which are particularly indicated when the final viewing conditions are known.

Concerning the superpixel segmentation, the threshold $t$ in equations (1) and (4), that is, the one to decide if two colors are different enough to be both added to the respective sets $I_{i}$ and $O_{i}$ or they have to be averaged into a single color, is set to $3 \Delta E$ units. Below this value, humans hardly perceive color differences. Concerning class labels, in all the examples equal-length labels are assumed. The size for the box filer $b_{i}$ and thus of the space reserved to the placement of the label of each region has been set to $[w, h]=[75,21]$.

In Figure 5 for each example, we report the original image, its segmentation with number overlaid representing the class id, and different proposals: the results using the gray-scale and iso-luminance palettes (with $\left[w_{d}, w_{A}, w_{I}, w_{O}\right]=\left[w_{d}, w_{A}, 0,0\right]$ and no labels overlaid), the results using the web-safe palette (with $\left[w_{d}, w_{A}, w_{I}, w_{O}\right]=\left[w_{d}, w_{A}, w_{I}, w_{O}\right]$ and labels overlaid) coloring boundaries only, or overlaying region colors


Figure 4. Colors selected for the three palettes for different set cardinalities $n=3,4,6,9,12$ without considering the spatial layout (top row) and their position inside the respective palettes (remaining rows). The sRGB coordinates of the selected colors are reported in Appendix 1.
on the original image. The RAG of each image is reported in Figure 6. Notice how for classes composed of multiple regions (i.e. class 4 in the first image, class 2 in the second one, and class 5 in the third one) the labels are placed on the region that can contain the whole label. Together with the different proposals, the user can also set the transparency level of the overlay solutions as well as the saturation of the underlying image. Some examples of the effect of these two parameters are shown in Figure 11 in Appendix 1.

In Figure 7, we report the chromaticity plane of the CIELab color space showing the position of the chosen colors with respect to image colors for the first image in Figure 5 using the web-safe palette. The image colors $I_{i}$ and $O_{i}$ for each class $r_{i}$ are represented as blue dots. The colors themselves are represented as red crosses. The gray line represents the boundary of
the CIELab color space and is a superset of the palette. From the figure, it is possible to see how the four selected colors are both very far from each other and far from the colors of the corresponding underlying classes.

Finally, we numerically compare the results obtained by the proposed algorithm with those obtained by two alternative solvers to the LS proposed in this article: the first one is a color selection and placement solution obtained by multiple random selections; the second one is based on GAs that are often used to solve high-contrast color selection problems. ${ }^{26}$ Concerning random selection, we performed $1,000,000$ random independent runs and report the results of both the best solution found and the average solution. Concerning GA, we performed 100 independent runs with 200 individuals each and report the results of both the best solution found and the average solution. The results are reported both in terms of fitness and in terms of the four elements of which it is composed of: the distance between colors $\left(d_{D}\right)$, the distance among adjacent colors ( $d_{A}$ ), and the distance among the color associated with each class and the colors, respectively, inside and outside of it ( $d_{I}$ and $d_{O}$ ). Results are visualized as radar plots in Figure 8. Note that $d_{D} \leqslant d_{A}$, and the equality holds only when the nearest colors are assigned to adjacent regions. From the plots, it is possible to see that the proposed method is able to outperform the compared solvers on all the sample images and on all the different terms composing the fitness function. The second best solution is always obtained by the best GA solution, with the average random solution obtaining the worst result. Numerical values for the fitness values are also reported in Table 2 together with the improvement of our solutions with respect to the best compared solver, that is, the best GA solution. In particular, we can observe that when the number of classes is small (i.e. 4 to 5) the average improvement of the proposed method with respect to the best GA solution is $2.43 \%$; when the number of classes increases, instead, the average improvement increases to $26.06 \%$. Computational times are reported in Table 3. For the best random solution, the total time for the $1,000,000$ guesses is reported, while for the average random one, the time for a single guess is reported. For the best GA solution, the total time for the 100 runs is reported, while for the average GA one, the time for a single run is reported. For the proposed method, being it not based on randomness, a single value is reported.

To test the robustness of the proposed method to the initialization, 100 independent runs are performed with random initialization. The radar plots of the solution obtained with the proposed initialization and the average solution obtained with random initialization


Figure 5. Examples of results obtained by our method: (a) original image, (b) its segmentation with overlaid region identification numbers, pseudo-color results using the (c) gray-scale palette and (d) iso-luminance palettes, and region boundaries (e) with and ( $f$ ) without overlaid colors using the web-safe palette (both with labels overlaid).
are reported in Figure 9. The average drop in performance using a random initialization is less than $6.5 \%$, which is one order of magnitude lower than the one that we have passing from the best random solution to the average random one (i.e. $66.8 \%$ ), and almost half of the one that we have passing from the best GA solution to the average GA one (i.e. $10.0 \%$ ). Furthermore, even with random initialization, the results obtained by the proposed method are on average almost $4.4 \%$
better than those obtained by the best GA solution, confirming the robustness of the proposed method to the choice of the initial conditions.

As a final experiment, we run the same experiments as before changing the working color space used from CIELab to CIECAM02-UCS. ${ }^{42}$ The CIECAM02UCS is an extension of CIECAM02 that better fits both small and large color differences. As mentioned at the beginning of this section, to be properly used,


Figure 6. RAGs of the images reported in Figure 5.


Figure 7. Chromaticity plane of the CIELab color space showing the position of the chosen colors with respect to image colors for the first image in Figure 5 using the web-safe palette. Image colors $I_{i}$ and $O_{i}$ for each class $r_{i}$ are represented as blue dots. The colors themselves are represented by red crosses. The gray line represents the boundary of the CIELab color space.

Table 2. Comparison of fitness values obtained in terms of CIELab $\Delta E$ by the random selection, the GA selection, and the proposed method on the five images in Figure 5.

| Image | No. of <br> classes | No. of <br> regions | Random <br> (best) | GA (best) | Random <br> laverage) | GA (average) | Proposed | Improvement |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: |
| Image 1 (horse) | 4 | 7 | 60.95 | 70.10 | 17.76 | 61.68 | 70.10 | $0.00 \%$ |
| Image 2 (texture) | 8 | 13 | 45.15 | 47.45 | 17.78 | 43.75 | 60.63 | $27.78 \%$ |
| Image 3 (Oscar) | 5 | 6 | 56.44 | 59.76 | 18.74 | 54.74 | 63.50 | $6.26 \%$ |
| Image 4 (basketball) | 4 | 5 | 61.90 | 69.02 | 18.34 | 62.12 | 69.74 | $1.03 \%$ |
| Image 5 (webpage) | 8 | 8 | 42.93 | 50.13 | 14.89 | 44.15 | 62.33 | $24.34 \%$ |

GA: genetic algorithm. For the random selection, the higher and the average fitness over 1,000,000 independent runs are reported. For the GA selection, the higher and the average fitness over 100 independent runs with 200 individuals each are reported.


Figure 8. Radar plot visualizations of the fitness values and the four terms of which it is composed, obtained by the random selection (red) and the proposed method (blue) on the five images in Figure 5. For the random selection, the higher fitness over 1000 independent runs is reported.

Table 3. Comparison of execution times for the random selection, the GA selection, and the proposed method on the five images in Figure 5.

| Image | No. of <br> classes | No. of <br> regions | Random <br> (best) | GA (best) | Random <br> laverage) | GA <br> (average) | Proposed |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | ---: |
| Image 1 (horse) | 4 | 7 | 1305.8 s | 1507.6 s | 0.0013 s | 15.08 s | 3.03 s |
| Image 2 (texture) | 8 | 13 | 2073.4 s | 2947.8 s | 0.0021 s | 29.48 s | 18.87 s |
| Image 3 (Oscar) | 5 | 6 | 1529.4 s | 1793.4 s | 0.0015 s | 17.93 s | 5.56 s |
| Image 4 (basketball) | 4 | 5 | 1349.2 s | 1481.4 s | 0.0013 s | 14.81 s | 3.22 s |
| Image 5 (webpage) | 8 | 8 | 2048.5 s | 3036.4 s | 0.0020 s | 30.36 s | 18.99 s |

GA: genetic algorithm.For the random selection, the average and total time for 1,000,000 independent runs are reported. For the GA selection, the average and total time for the 100 independent runs with 200 individuals each are reported.

CIECAM02 and its extensions require the final viewing conditions to be known and specified. We run the experiments considering two different viewing conditions: self-luminous display with CIE D65 white point under office illumination and print evaluation in a light booth under CIE D50 standard illuminant. The relevant parameters of both the viewing conditions are reported in Table 4 . The distance $d(\cdot, \cdot)$ used is the $\Delta E^{\prime}$, and the threshold $t$ is set to 3 units. The fitness
values are reported in Table 5, where it can be seen that algorithms' ranking are the same as those in Table 2 and the improvements are similar. Additionally, we replicate the results reported in Figure 4 by considering the CIECAM02-UCS color space and the viewing condition 1 (see Table 4). The results are reported in Figure 10 and represent the colors selected for the three palettes for different set cardinalities $n=3,4,6,9,12$ without considering the spatial


Figure 9. Radar plot visualizations of the fitness values and the four terms of which it is composed, obtained of the proposed method with the proposed initialization (solid line) and the average solution obtained with random initialization (dashed line) on the five images in Figure 5. For the random initialization, the average values over 100 independent runs are reported.

Table 4. Relevant parameters for the two viewing conditions considered in Table 5.

| Parameters | Viewing conditions |  |
| :--- | :--- | :--- |
|  | 1 | 2 |
| Ambient illumination in lux (or $\left.\mathrm{cd} / \mathrm{m}^{2}\right)$ | $500(159.2)$ | $1000(318.3)$ |
| Scene or device white luminance | 80 | 318.30 |
| $L_{A}$ in $\mathrm{cd} / \mathrm{m}^{2}$ | 15 | 60 |
| Adopted white point | Display | Light booth |
| $S_{R}$ | 2 | 1 |
| Surround | Average | Average |

layout, that is, setting $\left[w_{d}, w_{A}, w_{I}, w_{O}\right]=[1,0,0,0]$. The sRGB coordinates of the selected colors are also reported in Appendix 1 to allow their further visual appreciation and their immediate re-use.

## Conclusion

Color is pre-attentively observed and used to segment the visual environment. This characteristic makes it
particularly effective in visualizing image classification and segmentation results. A problem that may arise is that we often have more items to be represented in an image than easily discriminable colors. Moreover, selecting a high-contrast color subset is only part of the solution since the colors must be assigned to the image classes and displayed together. In this article, we proposed a general purpose system that given as input a segmented/classified image automatically provides

Table 5. Comparison of fitness values obtained in terms of CIECAMO2-UCS $\Delta E^{\prime}$ by the random selection, the GA selection, and the proposed method on the five images in Figure 5.

| Image | Viewing condition 1 |  |  |  | Viewing condition 2 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Random (best) | GA (best) | Proposed | Improvement | Random (best) | GA (best) | Proposed | Improvement |
| Image 1 (horse) | 72.64 | 72.09 | 74.76 | 2.92\% | 74.46 | 75.61 | 75.61 | 0.00\% |
| Image 2 (texture) | 36.22 | 41.02 | 50.23 | 22.45\% | 37.63 | 43.18 | 51.75 | 19.85\% |
| Image 3 (Oscar) | 55.25 | $\begin{aligned} & 60.41 \\ & 63.15 \end{aligned}$ | 4.54\% | 58.22 | 63.02 | 66.33 | 5.25\% |  |
| Image 4 (basketball) | 73.32 | 71.44 | 74.05 | 1.00\% | 74.96 | 74.52 | 75.12 | 0.21\% |
| Image 5 (webpage) | 34.98 | 43.43 | 52.87 | 21.74\% | 35.07 | 45.98 | $\begin{aligned} & 53.82 \\ & 17.95 \% \end{aligned}$ |  |

GA: genetic algorithm.For the random selection, the higher fitness over 1,000,000 independent runs is reported. For the GA selection, the higher fitness over 100 independent runs with 200 individuals each is reported.


Figure 10. Colors selected for the three palettes for different set cardinalities $n=3,4,6,9,12$ without considering the spatial layout (top row) and their position inside the respective palettes (remaining rows). The color space considered is the CIECAM02-UCS under the viewing condition 1 (see Table 1). The sRGB coordinates of the selected colors are reported in Appendix 1.
different types of outputs ranging from solutions to be used when a pseudo-color representation of the image is needed, to solutions to be used when region boundaries have to be displayed or transparent colors have to be overlaid on the original image, specifically: different pseudo-color representations (obtained using different color palettes), colored region boundaries displayed on the original image, transparent colors overlaid on the original image, and if available, the automatic placement of the class labels. Both the color selection and class-color association are formulated as an optimization problem and heuristically solved using a LS procedure. Experimental results show the effectiveness of the proposed method on images having different content and different number of annotated classes. Results are compared with the best solution obtained in 1000 independent random selections, showing an average improvement of $51.6 \%$ in the fitness values. Finally, we also included a method for the automatic placement of class labels on the image exploiting an image description in terms of saliency.

The proposed system is available at http://www.ivl.-disco.unimib.it/activities/cc4visual-im-class-results/ and could be used in existing image and video annotation software such as LabelMe, ${ }^{9}$ Ilastik, ${ }^{43}$ Sloth, ${ }^{44}$ VATIC, ${ }^{10}$ and iVat. ${ }^{11}$

As future work we plan to investigate the use of a combination of different image descriptions to better identify the less prominent sub-regions of the image. We also plan to conduct a user study to investigate where users prefer to place class labels and integrate these preferences directly in the fitness function. ${ }^{45}$ The whole system could be validated in specific use cases, for example, remote sensing where the color-class association should take into account the semantic and therefore the colors could be a priori fixed or limited to a certain portion of the gamut (e.g. we could be
interested to use a particular green for fields or limit the associated color to the gamut of greens). In the actual system, it is already possible to fix one or more colors, but this functionality should be extended. The system could be further extended to include also options for visually impaired and color-blind users. We also plan to conduct a user study to evaluate the proposed system and to integrate more complex relationships among the chosen colors such as color harmony. ${ }^{46}$

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## Appendix 1

In the following, we report the sRGB coordinates of the high-contrast colors selected in Figures 4 and 10 (Tables 6-11). We also report in Figure 11 some examples of the effect of setting the transparency level of the overlay solutions as well as the saturation of the underlying image.

Table 6. sRGB coordinates of the high-contrast colors selected in Figure 4 for the gray-scale palette using CIELab as the working color space.

| no. | R | G | B | R | G | B | R | G | B | R | G | B | R | G | B |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2 | 128 | 128 | 128 | 85 | 85 | 85 | 51 | 51 | 51 | 32 | 32 | 32 | 23 | 23 | 23 |
| 3 | 255 | 255 | 255 | 170 | 170 | 170 | 102 | 102 | 102 | 64 | 64 | 64 | 46 | 46 | 46 |
| 4 |  |  |  | 255 | 255 | 255 | 153 | 153 | 153 | 96 | 96 | 96 | 70 | 70 | 70 |
| 5 |  |  |  |  |  |  | 204 | 204 | 204 | 128 | 128 | 128 | 93 | 93 | 93 |
| 6 |  |  |  |  |  |  | 255 | 255 | 255 | 159 | 159 | 159 | 116 | 116 | 116 |
| 7 |  |  |  |  |  |  |  |  |  | 191 | 191 | 191 | 139 | 139 | 139 |
| 8 |  |  |  |  |  |  |  |  |  | 223 | 223 | 223 | 162 | 162 | 162 |
| 9 |  |  |  |  |  |  |  |  |  |  |  |  | 185 | 185 | 185 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |  | 209 | 209 | 209 |
| 11 |  |  |  |  |  |  |  |  | 232 | 232 |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Table 7. sRGB coordinates of the high-contrast colors selected in Figure 4 for the iso-luminance palette using CIELab as the working color space.

| no. | R | G | B | R | G | B | R | G | B | R | G | B | R | G | B |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 255 | 66 | 0 | 255 | 126 | 34 | 0 | 208 | 174 | 183 | 158 | 255 | 251 | 117 | 255 |
| 2 | 0 | 225 | 0 | 255 | 61 | 247 | 255 | 109 | 122 | 255 | 126 | 34 | 255 | 59 | 143 |
| 3 | 29 | 178 | 255 | 0 | 224 | 0 | 255 | 70 | 255 | 0 | 225 | 0 | 255 | 65 | 17 |
| 4 |  |  |  | 0 | 212 | 255 | 0 | 225 | 0 | 211 | 176 | 147 | 165 | 202 | 0 |
| 5 |  |  |  |  |  |  | 231 | 180 | 1 | 255 | 70 | 255 | 251 | 155 | 133 |
| 6 |  |  |  |  |  |  |  | 152 | 255 | 0 | 217 | 155 | 180 | 187 | 126 |
| 7 |  |  |  |  |  |  |  |  |  | 0 | 212 | 255 | 244 | 172 | 44 |
| 8 |  |  |  |  |  |  |  |  |  | 198 | 191 | 142 | 223 | 162 | 220 |
| 9 |  |  |  |  |  |  |  |  |  |  | 225 | 0 |  |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |  | 87 | 185 | 255 |
| 11 |  |  |  |  |  |  |  |  |  |  |  | 214 | 208 |  |  |
| 12 |  |  |  |  |  |  |  |  |  | 210 | 120 |  |  |  |  |

Table 8. sRGB coordinates of the high-contrast colors selected in Figure 4 for the web-safe palette using CIELab as the working color space.

| no. | R | G | B | R | G | B | R | G | B | R | G | B | R | G | B |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 255 | 0 | 0 | 204 | 255 | 0 | 0 | 0 | 255 | 255 | 0 | 0 | 102 | 0 |
| 2 | 255 | 0 | 0 | 204 | 0 | 0 | 255 | 0 | 153 | 255 | 0 | 0 | 153 | 0 | 51 |
| 3 | 0 | 0 | 255 | 0 | 255 | 0 | 0 | 153 | 255 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4 |  |  |  | 0 | 0 | 255 | 102 | 204 | 153 | 0 | 0 | 204 | 255 | 102 | 0 |
| 5 |  |  |  |  |  |  | 204 | 102 | 0 | 0 | 255 | 255 | 0 | 255 | 0 |
| 6 |  |  |  |  |  |  |  | 0 | 255 | 255 | 0 | 204 | 0 | 0 | 102 |
| 7 |  |  |  |  |  |  |  |  |  | 153 | 102 | 0 | 0 | 255 | 204 |
| 8 |  |  |  |  |  |  |  |  |  | 255 | 102 | 102 | 204 | 255 |  |
| 9 |  |  |  |  |  |  |  |  |  |  |  |  | 255 | 255 | 255 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |  | 0 | 0 | 255 |
| 11 |  |  |  |  |  |  |  |  |  |  |  | 255 | 204 | 153 |  |
| 12 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Table 9. sRGB coordinates of the high-contrast colors selected in Figure 10 for the gray-scale palette using CIECAM02UCS as the working color space under the viewing condition 1 (see Table 4).

| no. | R | G | B | R | G | B | R | G | B | R | G | B | R | G | B |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2 | 128 | 128 | 128 | 85 | 85 | 85 | 51 | 51 | 51 | 32 | 32 | 32 | 23 | 23 | 23 |
| 3 | 255 | 255 | 255 | 170 | 170 | 170 | 102 | 102 | 102 | 64 | 64 | 64 | 46 | 46 | 46 |
| 4 |  |  |  | 255 | 255 | 255 | 153 | 153 | 153 | 96 | 96 | 96 | 70 | 70 | 70 |
| 5 |  |  |  |  |  |  | 204 | 204 | 204 | 128 | 128 | 128 | 93 | 93 | 93 |
| 6 |  |  |  |  |  |  | 255 | 255 | 255 | 159 | 159 | 159 | 116 | 116 | 116 |
| 7 |  |  |  |  |  |  |  |  |  | 191 | 191 | 191 | 139 | 139 | 139 |
| 8 |  |  |  |  |  |  |  |  |  | 223 | 223 | 223 | 162 | 162 | 162 |
| 9 |  |  |  |  |  |  |  |  |  |  |  |  | 255 | 255 | 185 |
| 185 | 185 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |  | 209 | 232 | 232 |
| 11 |  |  |  |  |  |  |  |  |  | 232 |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |  |  |  |  | 255 | 255 | 255 |  |

Table 10. sRGB coordinates of the high-contrast colors selected in Figure 10 for the iso-luminance palette using CIECAM02-UCS as the working color space under the viewing condition 1 (see Table 4).

| no. | R | G | B | R | G | B | R | G | B | R | G | B | R | G | B |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 212 | 255 | 255 | 77 | 255 | 0 | 225 | 0 | 255 | 60 | 126 | 246 | 155 | 186 |
| 2 | 247 | 173 | 9 | 255 | 126 | 0 | 233 | 180 | 0 | 255 | 111 | 0 | 255 | 61 | 109 |
| 3 | 255 | 61 | 247 | 0 | 225 | 0 | 249 | 155 | 151 | 167 | 159 | 255 | 207 | 163 | 247 |
| 4 |  |  |  | 0 | 194 | 255 | 146 | 191 | 161 | 0 | 225 | 0 | 236 | 171 | 112 |
| 5 |  |  |  |  |  |  | 228 | 148 | 255 | 121 | 195 | 160 | 255 | 93 | 0 |
| 6 |  |  |  |  |  |  | 0 | 204 | 255 | 254 | 115 | 255 | 181 | 181 | 181 |
| 7 |  |  |  |  |  |  |  |  |  | 212 | 185 | 35 | 110 | 168 | 255 |
| 8 |  |  |  |  |  |  |  |  |  | 0 | 206 | 255 | 255 | 61 | 247 |
| 9 |  |  |  |  |  |  |  |  |  |  |  |  | 0 | 2185 | 242 |
| 10 |  |  |  |  |  |  |  |  |  |  |  |  | 0 | 214 | 156 |
| 11 |  |  |  |  |  |  |  |  |  |  |  |  |  | 195 | 190 |
| 12 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Table 11. sRGB coordinates of the high-contrast colors selected in Figure 10 for the web-safe palette using CIECAM02UCS as the working color space under the viewing condition 1 (see Table 4).

| no. | R | G | B | R | G | B | R | G | B | R | G | B | R | G | B |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 255 | 0 | 0 | 0 | 0 | 204 | 255 | 0 | 153 | 0 | 204 | 0 | 153 | 255 |  |
| 2 | 255 | 0 | 51 | 255 | 0 | 0 | 0 | 102 | 0 | 0 | 153 | 255 | 255 | 0 | 102 |  |
| 3 | 0 | 0 | 153 | 153 | 153 | 255 | 0 | 0 | 153 | 51 | 0 | 0 | 102 | 0 | 0 |  |
| 4 |  |  |  | 0 | 204 | 0 | 0 | 204 | 255 | 255 | 204 | 255 | 255 | 153 | 51 |  |
| 5 |  |  |  |  |  |  | 255 | 102 | 255 | 255 | 204 | 0 | 204 | 255 | 0 |  |
| 6 |  |  |  |  |  |  |  |  | 0 | 0 | 0 | 102 | 0 | 0 | 255 | 255 |
| 7 |  |  |  |  |  |  | 0 | 0 | 102 | 0 | 0 | 153 |  |  |  |  |
| 8 |  |  |  |  |  |  |  | 0 | 255 | 204 | 102 | 102 | 102 |  |  |  |
| 9 |  |  |  |  |  |  |  |  |  | 0 | 0 | 0 | 0 |  |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  | 255 | 204 | 255 |  |  |  |
| 11 |  |  |  |  |  |  |  |  |  |  | 153 | 0 | 204 |  |  |  |
| 12 |  |  |  |  |  |  |  |  | 0 | 153 | 0 |  |  |  |  |  |



Figure 11. Different proposals for the overlay solution using the web-safe palette. The transparency of the overlaid colors is changed in five steps (from $100 \%$ to $0 \%$ ) along the different columns; the saturation of the underlying image is changed in five steps (from $0 \%$ to 100\%) along the different rows.


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